

Multi-Functional Filtering Power Divider with a Reconfigurable Frequency and Ultrawide Isolator Functionality

Girdhari Chaudhary¹  · Daewoo Choi^{2,*}  · Yongchae Jeong^{1,3,*} 

Abstract

In this paper, we describe the co-design of a multi-functional non-reciprocal filtering power divider (NR-FPD) with ultrawide reverse isolation and frequency reconfigurable functionality. The proposed NR-FPD offers an arbitrary power division ratio (PDR) with low transmission loss in the forward direction and non-reciprocal behavior along with an ultrawide high reverse isolation bandwidth in the backward direction. For a better understanding of the behavior of the proposed NR-FPD, analytical equations of spectral S -parameters were derived. These equations allowed for the selection of optimum circuit and modulation parameters without the need for harmonic balance simulation. The ultrawide high reverse isolation bandwidth was achieved through the proper selection of optimum modulation parameters. For the proof of concept, the NR-FPD with an equal PDR was fabricated and characterized. Measurement results showed that the frequency was continuously tuned between 1.62 GHz to 1.95 GHz, and there was insertion loss of 5.70 dB in the forward direction of transmission and an ultrawide 20 dB isolation bandwidth in the backward direction of transmission.

Key Words: Frequency Reconfigurable, Non-Reciprocal Circuits, Non-reciprocal Power Divider, Spatio-temporal Modulation, Time-Modulated Resonators, Varactor Diode.

I. INTRODUCTION

Multi-functional microwave and millimeter wave circuits are essential components of next generation communication systems. Since emerging applications require multi-functional RF front ends, there is a pressing need for power dividers/combiners capable of accommodating these advancements [1, 2]. One promising approach for miniaturizing the RF front-end and enhancing functionality involves combining the power divider, tunable filter, and isolator functions into a single circuit. Circulators and isolators are

widely used in measurement, communication, and radar systems [3]. However, conventional circulators and isolators are mainly designed using a ferrite magnetic material [4], which is expensive, bulky, and incompatible with integrated circuit (IC) design.

In recent years, the spatio-temporal modulation (STM) technique has been widely used to design non-reciprocal circuits without the use of magnetic materials. Non-reciprocal bandpass filters (NR-BPFs) that integrate functionalities of isolators and filters using time-modulated resonators have been explored [5–13]. The STM concept has also been utilized to design non-

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reciprocal power dividers (i.e., $|S_{21}| \neq |S_{12}|$ and $|S_{31}| \neq |S_{13}|$) by employing a combination of static and time-modulated resonators [14, 15]. In [16, 17], non-reciprocal filtering power dividers (NR-FPDs) with tunable frequencies were presented.

However, these designs require at least six time-modulated resonators. The aforementioned NR-BPFs and power dividers have achieved excellent reverse isolation only at the center frequency (f_0). In [6, 10–12], an NR-BPFs yielded reverse isolation values of up to 40 dB at f_0 , however, the 20 dB reverse isolation bandwidth was very narrow. Similarly, NR-FPDs with improved isolation bandwidth have been presented in [16, 17]. However, the 20 dB isolation bandwidth of these NR-FPDs was in the range of 23–50 MHz.

This paper presents the design of a microstrip line NR-FPD that offers frequency tunable characteristics with ultrawide bandwidth isolator functionality. The proposed design features an equal and unequal power division ratio (PDR) with low transmission insertion loss (IL) and ultrawide high isolation in the backward direction. To achieve deep understanding of the proposed multi-functional NR-FPD's non-reciprocity behavior, the analytical spectral scattering parameters (S -parameters) of the microstrip line NR-FPD were derived. As a proof of concept, an equal PDR NR-FPD with ultrawide reverse isolation bandwidth and tunable frequency functionality was designed, fabricated, and measured.

II. DESIGN THEORY

1. Proposed Transmission Line Time-Modulated Resonator

Fig. 1(a) depicts a schematic of time-modulated resonator. The proposed time-modulated resonators consisted of a transmission with characteristic admittances of Y_2 , Y_1 , and Y_b , and electrical lengths of θ_c , θ_1 , θ_0 , and θ_b . The capacitor $C_v(t)$ was modulated with a sinusoidal modulation signal as follows:

$$C_v(t) = C_{v0}[1 + m\cos\{2\pi f_m t + (i-1)\Delta\varphi\}], \quad (1)$$

where f_m , $\Delta\varphi$, and m represent the modulation frequency, phase shift, and modulation index of the modulation signal [6], and C_{v0} denotes nominal capacitance. The modulation of the resonator with the sinusoidal signal resulted in intermodulation (IM) products at harmonic frequencies (i.e., $\omega + k\omega_m$ where $k_i = \dots, -2, -1, 0, +1, +2, \dots$). If the number of harmonics was N_{har} , then the input spectral admittance matrix of an i^{th} transmission time-modulated resonator was written as (2),

$$Y_{in,i}^{(p_1,p_2)} = j \begin{bmatrix} \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ \dots & B^{-2} & x^{-2} \frac{m}{2} C_{v0} e^{-j(i-1)\Delta\varphi} & 0 & 0 & 0 & \dots \\ \dots & x^{-1} \frac{m}{2} C_{v0} e^{j(i-1)\Delta\varphi} & B^{-1} & x^{-1} \frac{m}{2} C_{v0} e^{-j(i-1)\Delta\varphi} & 0 & 0 & \dots \\ 0 & 0 & x^0 \frac{m}{2} C_{v0} e^{j(i-1)\Delta\varphi} & B^0 & x^0 \frac{m}{2} C_{v0} e^{-j(i-1)\Delta\varphi} & 0 & \dots \\ 0 & 0 & 0 & x^{+1} \frac{m}{2} C_{v0} e^{j(i-1)\Delta\varphi} & B^{+1} & x^{+1} \frac{m}{2} C_{v0} e^{-j(i-1)\Delta\varphi} & \dots \\ 0 & 0 & 0 & 0 & x^{+2} \frac{m}{2} C_{v0} e^{j(i-1)\Delta\varphi} & B^{+2} & \dots \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots \end{bmatrix} \quad (2)$$

where $Y_{in,i}^{k_1,k_2}$ symbolizes the spectral admittance matrix at frequency components $\omega + k\omega_m$. The values of B^k , D_1 , D_2 , and x^k were expressed as follows:

$$B^n = Y_2 \frac{D_1 + Y_2 \tan(x^n \theta_c / \omega_{ref})}{Y_2 - D_1 \tan(x^n \theta_c / \omega_{ref})}, \quad (3a)$$

$$D_1 = Y_1 \frac{D_2 + Y_1 \tan(x^n \theta_1 / \omega_{ref})}{Y_1 - D_2 \tan(x^n \theta_1 / \omega_{ref})}, \quad (3b)$$

$$D_2 = \frac{x^n C_{v0} Y_1 \cot(x^n \theta_0 / \omega_{ref})}{Y_1 \cot(x^n \theta_0 / \omega_{ref}) - x^n C_{v0}} - Y_b \cot\left(\frac{x^n \theta_b}{\omega_{ref}}\right), \quad (3c)$$

$$x^n = \omega + n\omega_m, \quad n = \dots, -2, -1, 0, +1, +2, \dots \quad (3d)$$

where ω_{ref} is an angular frequency at which the electrical length of transmission is chosen. As depicted in Eq. (2), it is important to emphasize that the spectral admittance matrix no longer held a singular value. The resonant frequency at the fundamental frequency (i.e., $n = 0$) was obtained by equating $\text{im}(Y_{in,i}^{0,0})$ to zero.

2. Spectral S -Parameters

Fig. 1(b) shows a schematic of the NR-FPD with an arbitrary PDR, comprised of admittance inverters and time-modulated resonators. The RF ports of the NR-FPD were terminated with the admittance of $Y_0 = 1/Z_0 = 0.02 \Omega$. To determine the spectral S -parameters of the proposed NR-FPD, modified even- and odd-mode analysis methods were adapted. Assuming that the input signal was divided between the output ports in a ratio of $1:k^2$, the spectral S -parameters of the entire circuit were expressed in terms of the even- and odd-mode S -parameters, as follows:

$$[S] = \begin{bmatrix} S_{11e}^{(p_1,p_2)} & \frac{k S_{12e}^{(p_1,p_2)}}{\sqrt{1+k^2}} & \frac{S_{13e}^{(p_1,p_2)}}{\sqrt{1+k^2}} \\ \frac{k S_{21e}^{(p_1,p_2)}}{\sqrt{1+k^2}} & k^2 \left(\frac{S_{22e}^{(p_1,p_2)} + S_{22o}^{(p_1,p_2)}}{1+k^2} \right) & \frac{S_{22e}^{(p_1,p_2)} - S_{22o}^{(p_1,p_2)}}{2} \\ \frac{S_{31e}^{(p_1,p_2)}}{\sqrt{1+k^2}} & \frac{S_{33e}^{(p_1,p_2)} - S_{33o}^{(p_1,p_2)}}{2} & \frac{S_{11e}^{(p_1,p_2)} + S_{33o}^{(p_1,p_2)}}{1+k^2} \end{bmatrix} \quad (4)$$

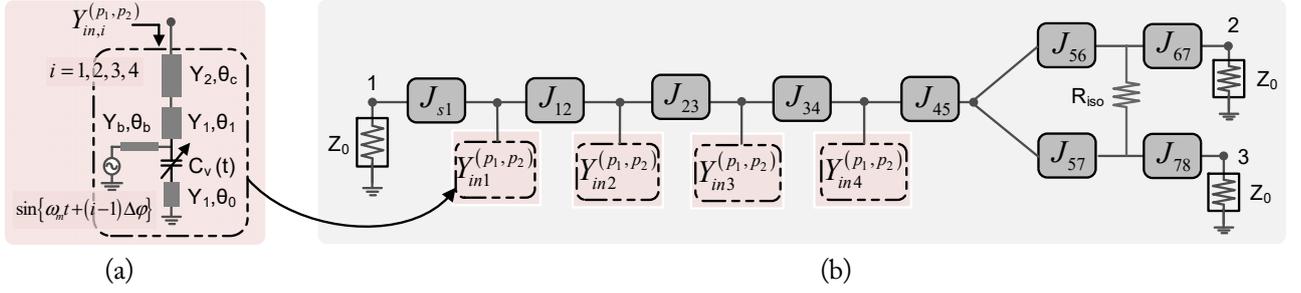


Fig. 1. Proposed structure: (a) a time-modulated resonator and (b) an NR-FPD with microstrip line time-modulated resonators and admittance inverters.

As seen in Eq. (4), the S -parameter $S_{i,j}^{(p_1,p_2)}$ did not possess a single value. Instead, it represented a spectral harmonic scattering matrix at the frequency of interest. For example, $S_{21}^{(0,0)} = S_{21}$ presented a transmission scattering parameter at port 2 at a fundamental frequency.

Figs. 2 and 3 show equivalent schematics for ports 2 and 1, and ports 3 and 1, respectively, under even- and odd-mode excitations. Under the even-excitations, the port 1 impedance was divided into $\left(\frac{1+k^2}{k^2}\right)Z_0$ and $(1+k^2)Z_0$. However, this impedance was short-circuited under the odd-mode excitation. Similarly, the input admittance of time-modulated resonators was divided into $\left(\frac{k^2}{1+k^2}\right)Y_{in,i}^{(p_1,p_2)}$ and $\left(\frac{1}{1+k^2}\right)Y_{in,i}^{(p_1,p_2)}$. Using equivalent circuits, as depicted in Fig. 2, the even- and odd-mode spectral S -parameters between ports 2 and 1 were expressed in the following equations, where U is unitary matrix.

$$S_{11e}^{(p_1,p_2)} = S_{22e}^{(p_1,p_2)} = U - \frac{2Z_0 J_{s1}^2 \left\{ \begin{array}{l} k^2 Z_0 J_{45}^2 J_{67}^2 A_3 \\ + (1+k^2) J_{56}^2 A_4 \end{array} \right\}}{\left\{ \begin{array}{l} k^2 Z_0 J_{45}^2 J_{67}^2 A_1 + (1+k^2) J_{56}^2 A_2 \\ + k^2 Z_0^2 J_{s1}^2 J_{45}^2 J_{67}^2 A_3 \\ + (1+k^2) Z_0 J_{s1}^2 J_{56}^2 A_4 \end{array} \right\}} \quad (5a)$$

$$S_{22o}^{(p_1,p_2)} = \frac{U - R_{iso}^{21} Z_0 J_{67}^2}{U + R_{iso}^{21} J_{67}^2}, \quad (5b)$$

$$S_{21e}^{(p_1,p_2)} = \frac{\sqrt{1+k^2}}{k} \frac{2k^2 Z_0 J_{s1} J_{12} J_{23} J_{34} J_{45} J_{56} J_{67}}{\left\{ \begin{array}{l} k^2 J_{45}^2 J_{67}^2 A_1 Z_0 + (1+k^2) J_{56}^2 A_2 \\ + k^2 Z_0^2 J_{s1}^2 J_{56}^2 J_{67}^2 A_3 + (1+k^2) Z_0 J_{s1}^2 J_{56}^2 A_4 \end{array} \right\}} \quad (5c)$$

$$S_{12e}^{(p_1,p_2)} = \frac{\sqrt{1+k^2}}{k} \frac{2k^2 Z_0 J_{s1} J_{12} J_{23} J_{34} J_{45} J_{56} J_{67}}{\left\{ \begin{array}{l} k^2 J_{45}^2 J_{67}^2 B_1 Z_0 + (1+k^2) J_{56}^2 B_2 \\ + k^2 Z_0^2 J_{s1}^2 J_{45}^2 J_{67}^2 B_3 + (1+k^2) Z_0 J_{s1}^2 J_{56}^2 B_4 \end{array} \right\}} \quad (5d)$$

Similarly, Fig. 3 depicts equivalent circuits between ports 3 and 1 when even- and odd-mode excitations were applied. Us-

ing these equivalent circuits, even- and odd-mode spectral reflection and transmission coefficients were derived as follows:

$$S_{33e}^{(p_1,p_2)} = U - \frac{2Z_0 J_{s1}^2 \left\{ \begin{array}{l} Z_0 J_{45}^2 J_{78}^2 A_3 + (1+k^2) Z_0 J_{57}^2 A_4 \end{array} \right\}}{\left\{ \begin{array}{l} Z_0 J_{45}^2 J_{78}^2 A_1 + (1+k^2) J_{57}^2 A_2 \\ + Z_0^2 J_{s1}^2 J_{45}^2 J_{78}^2 A_3 + (1+k^2) Z_0 J_{s1}^2 J_{57}^2 A_4 \end{array} \right\}} \quad (6a)$$

$$S_{31e}^{(p_1,p_2)} = \frac{2Z_0 \sqrt{1+k^2} J_{s1} J_{12} J_{23} J_{34} J_{45} J_{57} J_{78}}{\left\{ \begin{array}{l} Z_0 J_{45}^2 J_{78}^2 A_1 + (1+k^2) J_{57}^2 A_2 \\ + Z_0^2 J_{s1}^2 J_{45}^2 J_{78}^2 A_3 + (1+k^2) Z_0 J_{s1}^2 J_{57}^2 A_4 \end{array} \right\}} \quad (6b)$$

$$S_{13e}^{(p_1,p_2)} = \frac{2Z_0 \sqrt{1+k^2} J_{s1} J_{12} J_{23} J_{34} J_{45} J_{57} J_{78}}{\left\{ \begin{array}{l} k^2 J_{45}^2 J_{78}^2 B_1 Z_0 + (1+k^2) J_{57}^2 B_2 \\ + k^2 Z_0^2 J_{s1}^2 J_{45}^2 J_{78}^2 B_3 + (1+k^2) Z_0 J_{s1}^2 J_{57}^2 B_4 \end{array} \right\}} \quad (6c)$$

$$S_{33o}^{(p_1,p_2)} = \frac{U - R_{iso}^{31} Z_0 J_{78}^2}{U + R_{iso}^{31} Z_0 J_{78}^2}. \quad (6d)$$

The values of A_i and B_i were expressed as follows:

$$A_1 = J_{12}^2 Y_{in3}^{(p_1,p_2)} + J_{23}^2 Y_{in1}^{(p_1,p_2)} + Y_{in1}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)}, \quad (7a)$$

$$A_2 = \left\{ \begin{array}{l} J_{12}^2 J_{34}^2 + J_{12}^2 Y_{in3}^{(p_1,p_2)} Y_{in4}^{(p_1,p_2)} + J_{23}^2 Y_{in1}^{(p_1,p_2)} Y_{in4}^{(p_1,p_2)} \\ + J_{34}^2 Y_{in1}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)} + Y_{in1}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)} Y_{in4}^{(p_1,p_2)} \end{array} \right\} \quad (7b)$$

$$A_3 = J_{23}^2 + Y_{in2}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)}, \quad (7c)$$

$$A_4 = J_{23}^2 Y_{in4}^{(p_1,p_2)} + J_{34}^2 Y_{in2}^{(p_1,p_2)} + Y_{in2}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)} Y_{in4}^{(p_1,p_2)}, \quad (7d)$$

$$B_1 = J_{12}^2 Y_{in3}^{(p_1,p_2)} + J_{23}^2 Y_{in1}^{(p_1,p_2)} + Y_{in3}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)} Y_{in1}^{(p_1,p_2)}, \quad (7e)$$

$$B_2 = \left\{ \begin{array}{l} J_{12}^2 J_{34}^2 + J_{12}^2 Y_{in4}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)} + J_{23}^2 Y_{in4}^{(p_1,p_2)} Y_{in1}^{(p_1,p_2)} \\ + J_{34}^2 Y_{in2}^{(p_1,p_2)} Y_{in1}^{(p_1,p_2)} + Y_{in4}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)} Y_{in1}^{(p_1,p_2)} \end{array} \right\} \quad (7f)$$

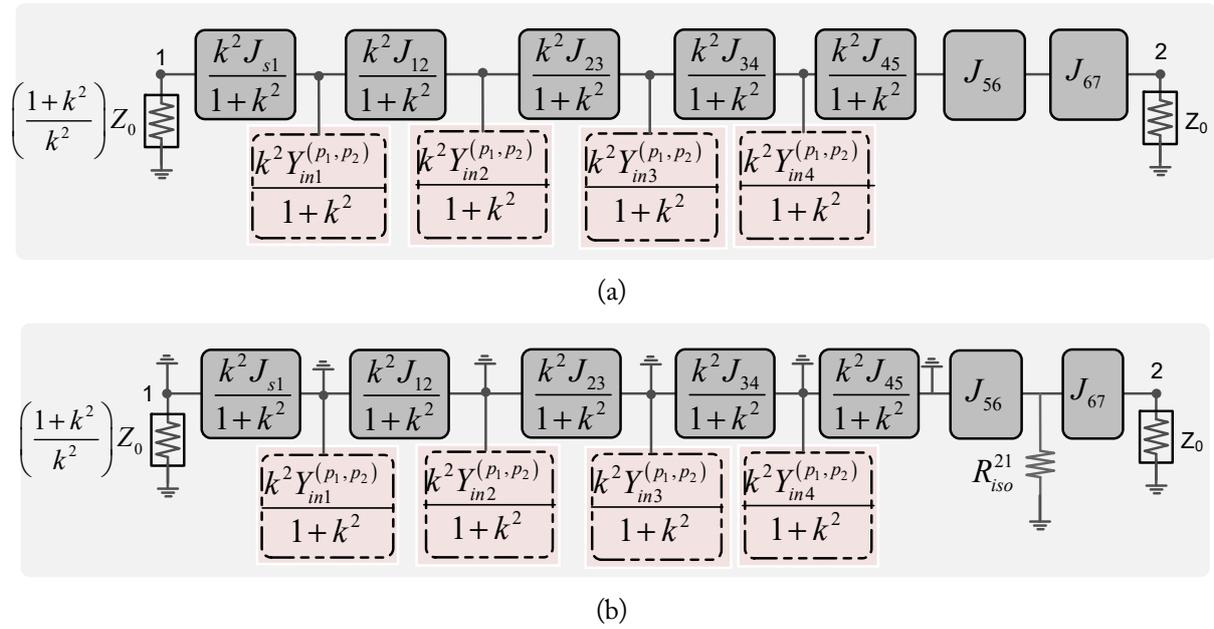


Fig. 2. Even- and odd-mode equivalent circuits between ports 2 and 1: (a) an even-mode equivalent circuit and (b) an odd-mode equivalent circuit.

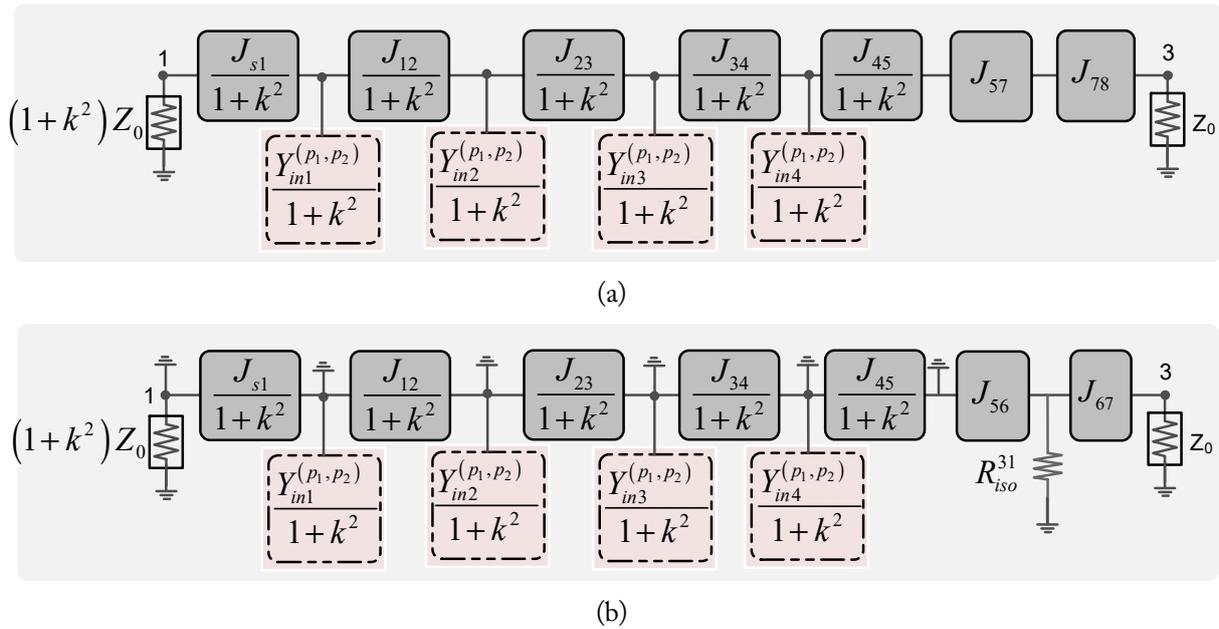


Fig. 3. Equivalent circuits under even- and odd-mode excitations between ports 3 and 1: (a) an even-mode equivalent circuit and (b) an odd-mode equivalent circuit.

$$B_3 = J_{23}^2 + Y_{in3}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)}, \quad (7g)$$

$$B_4 = J_{23}^2 Y_{in4}^{(p_1,p_2)} + J_{34}^2 Y_{in2}^{(p_1,p_2)} + Y_{in4}^{(p_1,p_2)} Y_{in3}^{(p_1,p_2)} Y_{in2}^{(p_1,p_2)}. \quad (7h)$$

It should be noted that admittance inverters (J-inverters) value remained same as they were without modulation (i.e., in the static state) [6, 8]. The J-inverter values were expressed as follows:

$$J_{s1} = \sqrt{\frac{\Delta b_1^{(0,0)} U}{Z_0 g_0 g_1}}, \quad J_{45} = \sqrt{\frac{\Delta b_4^{(0,0)} U}{Z_0 g_4 g_5}}, \quad (8a)$$

$$J_{i,i+1} = \Delta \sqrt{\frac{b_i^{(0,0)} b_{i+1}^{(0,0)} U}{Z_0 g_1 g_2}}, \quad i = 1, 2, 3 \quad (8b)$$

$$J_{56} = \sqrt{\frac{k^2 U}{Z_0^2 (1+k^2)}}, \quad J_{67} = \frac{U}{Z_0}, \quad (8c)$$

$$J_{57} = \frac{U}{\sqrt{Z_0^2 (1+k^2)}}, \quad J_{78} = \frac{U}{\sqrt{k^2 Z_0}}, \quad (8d)$$

where g_i denotes either Chebyshev or Butterworth filter pro-

prototype values [18], and Δ represents the fractional bandwidth of NRF-FPD at static state (without modulation). Similarly, $b_i^{(0,0)}$ represents the slope parameters of the time-modulated resonator at the resonant frequency (ω_0). The value of $b_i^{(0,0)}$ at ω_0 was expressed as follows:

$$b_i^{(0,0)} = \frac{\omega_0}{2} \left. \frac{d[\text{im}(Y_{ini}^{0,0})]}{d\omega} \right|_{\omega=\omega_0} \quad (9)$$

To achieve perfect isolation between the outputs at f_0 , the value of the isolation resistor ($R_{iso} = R_{iso}^{21} + R_{iso}^{31}$) was calculated by equating $\mathbf{S}_{22o}^{(k_1, k_2)}$ and $\mathbf{S}_{33o}^{(k_1, k_2)}$ to zero. The values of R_{iso}^{21} and R_{iso}^{31} were expressed as follows:

$$R_{iso}^{2,1} = Z_0, \quad R_{iso}^{3,1} = k^2 Z_0. \quad (10)$$

As seen in Eq. (5c)–(5d) and Eq. (6a)–(6d), the proposed power divider split the signal transmission between the output ports with an arbitrary PDR (i.e., $|S_{21}| = k/\sqrt{1+k^2}$, $|S_{31}| = 1/\sqrt{1+k^2}$) in the forward direction and those with a high reverse isolation (i.e., $|S_{12}| = |S_{13}| \approx 0$) in the backward direction. The time-modulated resonator generated IM products due to the mixing of the RF and modulation signals. These IM products transmitted through different transmission paths with distinct transmission phases. The phase difference ($\Delta\varphi$) in the progressive phase shift sinusoidal modulation played an important role in attaining a non-reciprocal response. In the absence of a modulation signal, the proposed circuit functions acted like a conventional reciprocal power divider (i.e., $|S_{21}| = |S_{12}| = k/\sqrt{1+k^2}$, $|S_{31}| = |S_{13}| = 1/\sqrt{1+k^2}$).

3. Modulation Parameter Selection

With the appropriate selection of modulation parameters (i.e., f_m , m , $\Delta\varphi$), the proposed power divider achieved low transmission loss in the forward direction and high reverse isolation in the backward direction. To achieve low transmission loss and high reverse isolation, parametric studies of the modulation parameters were performed, and the results are shown in Fig. 4. These results in Fig. 4 were obtained using the analytical design equations described in previous sections. The chosen circuit parameters of time-modulated resonators $Z_1 = 70 \Omega$, $Z_2 = 60 \Omega$, $Z_b = 90 \Omega$, $\theta_0 = 16^\circ$, $\theta_1 = 40^\circ$, $\theta_c = 25^\circ$, and $C_{v0} = 6$ pF, resulted in a resonant frequency of 1.80 GHz. The low pass prototype elements were calculated by considering a return loss of 26.40 dB in the Chebyshev response. The modulation parameters and results are summarized in Table 1. As shown in the Fig. 4, the proposed NR-FPD exhibited a filtering response with low IL in the forward direction and high isolation (ISO) in the backward direction.

When the modulation parameters were $f_m = 89.64$ MHz, $m = 0.01543$, and $\Delta\varphi = 60^\circ$, a reverse ISO (i.e., $|S_{12}|$ and $|S_{13}|$) of higher than 45 dB was achieved at center frequency, however, the 20-dB ISO bandwidth is very narrow. When the modulation parameters were $f_m = 93.96$ MHz, $m = 0.01984$, and $\Delta\varphi = 32^\circ$, the forward transmission IL (IL = $|S_{21}| = |S_{31}|$) in the forward direction was less than 0.84 dB (excluding the inherent PDR of power divider), the input port return loss ($|S_{11}|$) at passband exceeded 14 dB, and the isolation in the backward direction (i.e., $|S_{12}|$ and $|S_{13}|$) remained higher than 18 dB for RF frequencies from 1.5 GHz to 2.1 GHz. Although the NR-FPD did not contain any lossy elements, the small IL was attributable due to the power conversion into IM products at harmonics, which was not fully recovered to the fundamental frequency.

As depicted in Fig. 4(b) and 4(c), the backward transmission isolation bandwidth of 17 dB of the proposed NR-FPD was infinite. It should be noted that ultrawide reverse ISO bandwidth was attained when $\Delta\varphi = 32^\circ$. Fig. 5 shows the calculated frequency response for the NR-FPD with different fractional bandwidths. These results indicated that if a higher fractional bandwidth of NR-FPD is chosen, then higher values for the modulation frequency (f_m) and modulation index (m) should also be chosen.

The simulated results for the proposed NR-FPD shown in Fig. 6, demonstrate tunable frequency response. The frequency tunable response can be attained by adjusting the capacitor values (C_{v0}). The modulation parameters and the summary of simulated S -parameters are presented in Table 2. The frequency tunable range was from 1.64 GHz to 1.98 GHz with a worst-case IL (excluding the intrinsic loss of power divider) that was below 0.82 dB. In addition, the reverse ISO exceeded 18.4 dB across the entire operating frequency span.

III. SIMULATION AND MEASUREMENT RESULTS

For the experimental proof-of-concept, an NR-FPD with an equal PDR ($k^2 = 1$) was designed and fabricated. The NR-FPD prototype was fabricated using a Taconic substrate with a thickness of $h = 0.787$ mm and a dielectric constant of $\epsilon_r = 2.2$. The proposed NR-FPD was designed with a fractional bandwidth of 6% and a passband return of 26.10 dB in the static state. The design objective was to obtain minimum IL and ultrawide high isolation in the backward direction while tuning the frequency from 1.60 GHz to 2 GHz. The time-modulated resonator was implemented by using transmission terminated with SMV1233-079LF varactor diode developed by Skyworks Inc. [19].

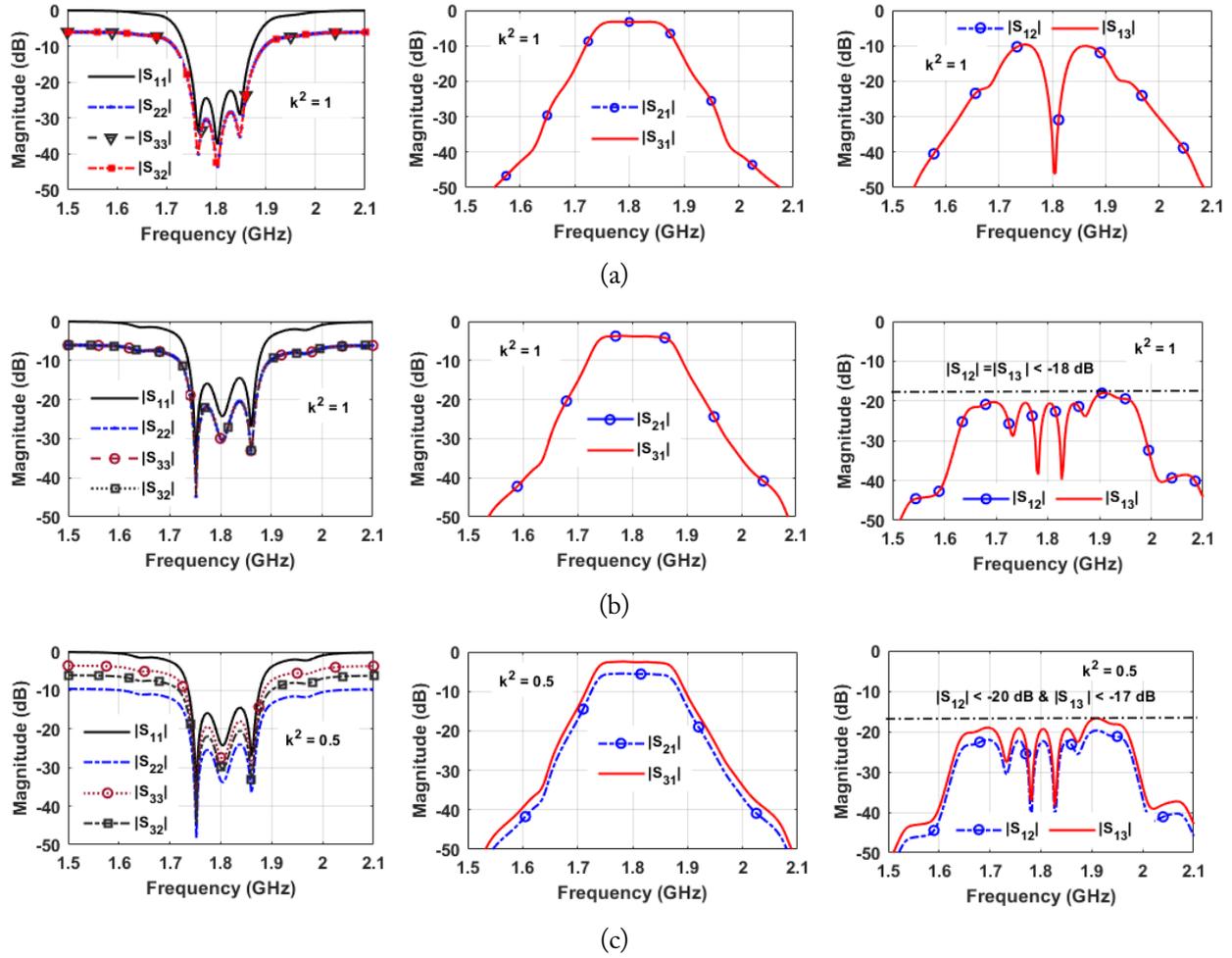


Fig. 4. Simulated S -parameters of the NR-FPD with various modulation parameters and power division ratios: (a) $k^2 = 1$, $f_m = 89.64$ MHz, $m = 0.01543$, $\Delta\varphi = 60^\circ$, (b) $k^2 = 1$, $f_m = 93.96$ MHz, $m = 0.01984$, $\Delta\varphi = 32^\circ$, and (c) $k^2 = 0.5$, $f_m = 93.96$ MHz, $m = 0.01984$, $\Delta\varphi = 32^\circ$. The chosen prototype element values were: $g_0 = 1.0$, $g_1 = 0.7127$, $g_2 = 1.20041$, $g_3 = 1.32131$, $g_4 = 0.6477$, $g_5 = 1.10061$. The J-inverter values for $k^2 = 1$ and $\Delta = 6\%$ were as follows: $J_{s1} = J_{45} = 0.0050741$, $J_{12} = J_{34} = 9.91939 \times 10^{-4}$, $J_{23} = 7.2855 \times 10^{-4}$, $J_{56} = J_{57} = 0.01414$, and $J_{67} = J_{78} = 0.02$. The J-inverter values for $k^2 = 0.5$ and $\Delta = 6\%$ were as follows: $J_{s1} = J_{45} = 0.0050741$, $J_{12} = J_{34} = 9.91939 \times 10^{-4}$, $J_{23} = 7.2855 \times 10^{-4}$, $J_{56} = 0.011547$, $J_{67} = 0.023094$, $J_{57} = 0.02$, and $J_{78} = 0.02828$.

Table 1. Modulation parameters and summary of the simulated results

PDR	Fractional BW, Δ (%)	Modulation parameters			$ S_{31} $ and $ S_{21} $ (dB)	$ S_{13} $ and $ S_{12} $ within the passband (dB)	ISO BW (MHz)	
		f_m (MHz)	m	$\Delta\varphi$			BW _{20dB-ISO}	BW _{18dB-ISO}
$k^2 = 1$	6	89.64	0.01543	60°	3.27 / 3.27	>10 / 10	36	51
		93.96	0.01984	32°	3.82 / 3.82	>20 / 20	200	∞
	4	63.34	0.01310	32°	3.82 / 3.82	>20 / 20	220	∞
$k^2 = 0.5$	6	99.1	0.01984	32°	2.60 / 5.60	>19.5 / 20	200	∞

BW_{20dB-ISO}=bandwidth of $|S_{12}|$ and $|S_{13}|$ when their values were less than -20 dB, BW_{18dB-ISO}=bandwidth of $|S_{12}|$ and $|S_{13}|$ when their values were less than -18 dB.

Fig. 7 shows the overall circuit implementation of the proposed NR-FPD. J-inverters, namely J_{s1} and J_{45} , were implemented using series transmission (W_a , L_a) and a coupled line (W_1 , L_1 , g_1). Similarly, coupling between the second and third

resonators (J_{12}) and between the third and fourth resonators (J_{34}) was implemented using a short-circuited transmission (W_g , L_g). Additionally, the coupling between the second and third resonators was implemented using a coupled line (W_4 , L_1 , g_2).

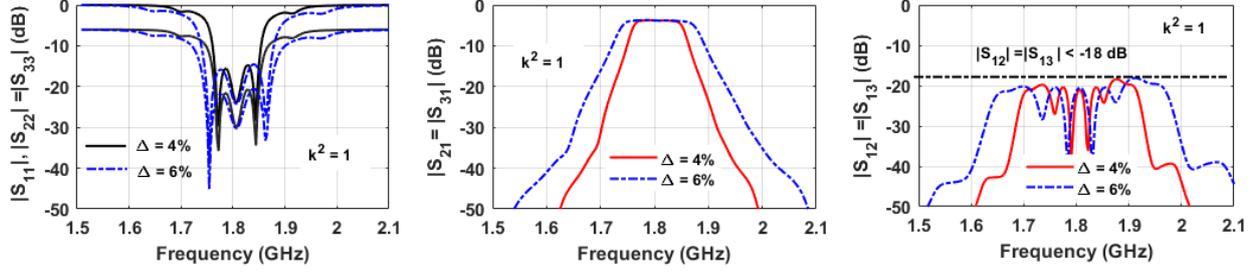


Fig. 5. Calculated S -parameters of NR-FPD with $k^2 = 1$ and various fractional bandwidths. The modulation parameters were $f_m = 93.96$ MHz, $m = 0.01984$, and $\Delta\phi = 32^\circ$. The chosen prototype element values were as follows: $g_0 = 1.0$, $g_1 = 0.71271$, $g_2 = 1.2004$, $g_3 = 1.32131$, $g_4 = 0.64771$, and $g_5 = 1.10061$. The J-inverter values were follows: $J_{s1} = J_{s5} = 0.0050741$, $J_{12} = J_{34} = 9.91939 \times 10^{-4}$, $J_{23} = 7.2855 \times 10^{-4}$, $J_{s6} = J_{s7} = 0.01414$, and $J_{67} = J_{78} = 0.02$.

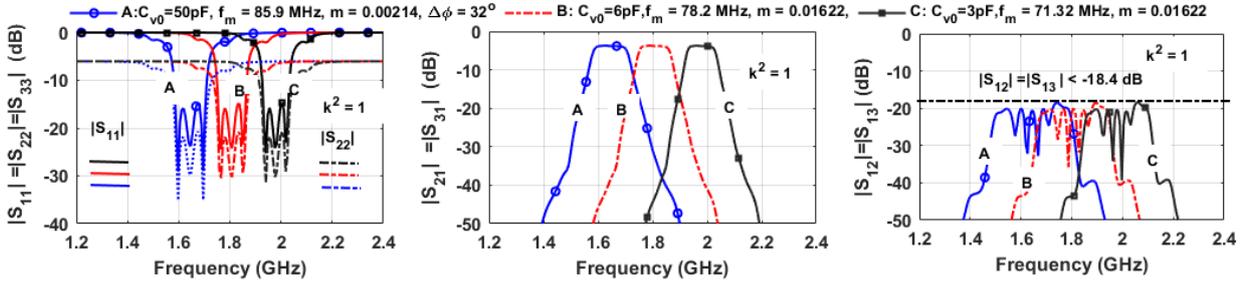


Fig. 6. Calculated S -parameters of NR-FPD with $k^2 = 1$ and frequency tunable characteristics. The chosen prototype values were as follows: $g_0 = 1.00$, $g_1 = 0.71271$, $g_2 = 1.20041$, $g_3 = 1.32131$, $g_4 = 0.64771$, and $g_5 = 1.10061$. The J-inverter values were as follows: $J_{s1} = J_{s5} = 0.0050741$, $J_{12} = J_{34} = 9.91939 \times 10^{-4}$, $J_{23} = 7.2855 \times 10^{-4}$, $J_{s6} = J_{s7} = 0.01414$, and $J_{67} = J_{78} = 0.02$.

Table 2. Modulation parameters and summary of the simulated results

PDR	C_{v0} (pF)	Modulation parameters			f_0 (GHz)	$ S_{21} / S_{31} $ (dB)	Reverse ISO = $ S_{12} = S_{13} $ the within passband (dB)	ISO BW (MHz)	
		f_m (MHz)	m	$\Delta\phi$				$BW_{20dB-ISO}$	$BW_{18dB-ISO}$
$k^2 = 1$	3	85.9	0.00214	32°	1.64	3.79 / 3.29	>20	36	∞
	6	78.02	0.01622	32°	1.81	3.78 / 3.78	>20	220	∞
	50	71.32	0.02978	32°	1.98	3.82 / 3.82	>20	200	∞

ISO=isolation, $BW_{20dB-ISO}$ =bandwidth of $|S_{12}|$ and $|S_{13}|$ when their values were less than -20 dB, $BW_{18dB-ISO}$ =bandwidth of $|S_{12}|$ and $|S_{13}|$ when their values were less than -18.4 dB.

Quarter-wavelength transmissions (W_p , L_p) were utilized for implementing J-inverters J_{s6} and J_{s7} . In addition, another quarter-wavelength TLs (W_0 , L_0) were employed to implement J-inverters J_{67} and J_{78} . The DC-bias voltage and the progressive phase shift sinusoidal modulation signal were applied to the varactor diode through transmission (TL_{bias} : W_5 and L_5), as shown in Fig. 7. The simulation results were obtained using the ANSYS high frequency structure simulator and Keysight Advanced System Design (ADS). The equivalent circuit model of the SMV1233-079LF varactor diode provided by manufacture was used in harmonic balance simulation. For the measurement, the DC-bias voltage and sinusoidal modulation signals were supplied to the NR-FPD circuit using 33622A Keysight arbitrary wave generators, where the DC-bias voltage and phase shift of the modulation signals could be easily controlled.

The frequency response of the fabricated prototype was characterized by measuring the S -parameter results. Fig. 8 shows the measurement setup for the NR-FPD. The comparison between the simulation and experimental S -parameters of NR-FPD is depicted in Fig. 9. As shown in the figures, the experimentally characterized S -parameters were well aligned with the simulations. The measured S -parameters results are summarized in Table 3.

Although Fig. 9 depicts the S -parameters of the fabricated NR-FPD at three tunable frequency states (A, B, and C) only, it should be noted that the frequency response of the fabricated NR-FPD was altered between 1.620 GHz and 1.950 GHz by varying the bias voltage of the varactor diode. The measurement results show that the passband input return loss ($|S_{11}|$) remained higher than 12 dB, output return losses ($|S_{22}|$ and $|S_{33}|$) were

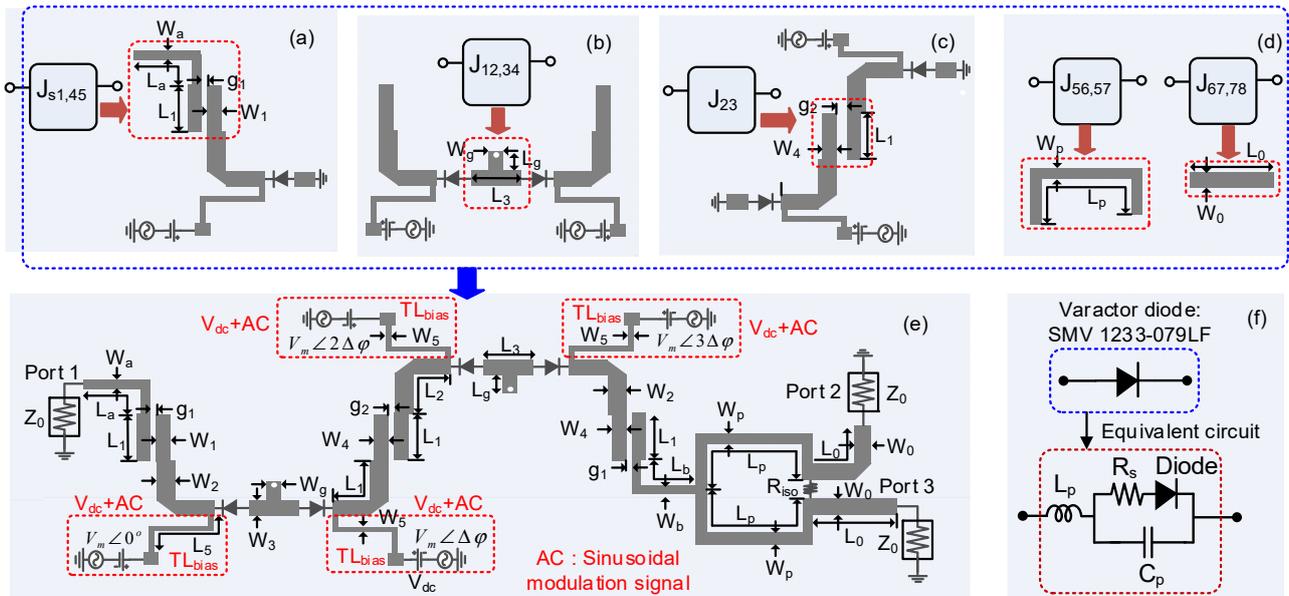


Fig. 7. Physical implementation of the NR-FPD with following dimensions: $W_a = W_b = 0.91$, $L_a = L_b = 12.21$, $g_1 = 0.12$, $W_1 = 1.04$, $L_1 = 10.78$, $W_2 = 1.37$, $L_2 = 16.02$, $L_3 = 11.96$, $W_g = 1.41$, $L_g = 1.51$, $W_4 = 1.72$, $g_2 = 1.13$, $W_5 = 0.61$, $L_5 = 24.10$, $W_p = 1.32$, $L_p = 32$, $W_0 = 2.40$, and $L_0 = 20$. The equivalent SPICE circuit model of the SMV1233-079LF varactor diode from Skyworks Inc. had parasitic resistance $R_s = 1.5 \Omega$, inductance $L_p = 0.7 \text{ nH}$, and $C_p = 0.5 \text{ pF}$.

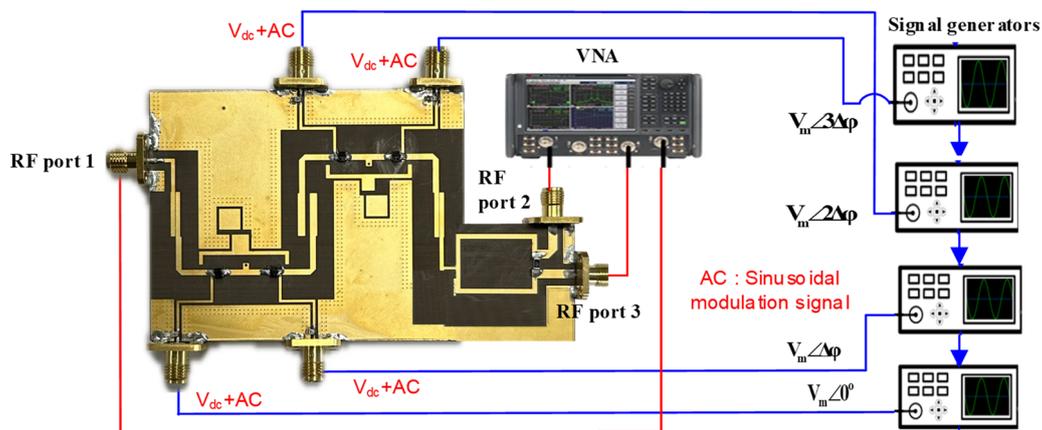


Fig. 8. Photograph of the fabricated NR-FPD with the measurement setup.

better than 15 dB and reverse ISO exceeded 19 dB. The transmission loss remained in the range of 4.31–5.41 dB (excluding the inherent 3.01 dB power division). These transmission losses occurred due to the parasitic resistance of varactor diodes. The parasitic resistance of the varactor diode increased at lower DC-bias voltages, causing the forward loss to increase slightly, while the frequency was tuned toward a lower frequency. The measurement also showed that the isolation of the two output ports (i.e., $|S_{32}|$) was higher than 16 dB at the passband center frequencies. Due to cross-coupling resulting from the progressive phase shifted sinusoidal modulation signal, transmission zeros (TZs) appeared in the forward direction of transmission, as shown in Fig. 9. When resonators were modulated with the progressive phase shift sinusoidal signal, IM products were gen-

erated. As a result, the RF power signal was distributed among the IM products, and transversal propagation of the RF signal occurred not only through the fundamental frequency, but also through non-adjacent resonators at harmonic frequencies. This phenomenon led to the generation of TZs.

To investigate the cause of the forward transmission IL, we performed a simulation of the NR-FPD using the SPICE model of SMV 1233-079LF varactor diode from Skyworks Inc. The results shown in Fig. 10 indicate that the forward transmission IL was mainly due to the parasitic resistance (R_s) of the varactor diode. As the value of R_s increased, the forward transmission IL also increased. Therefore, the IL can be reduced if a varactor diode with lower parasitic resistance (high Q -factor varactor diode) is used.

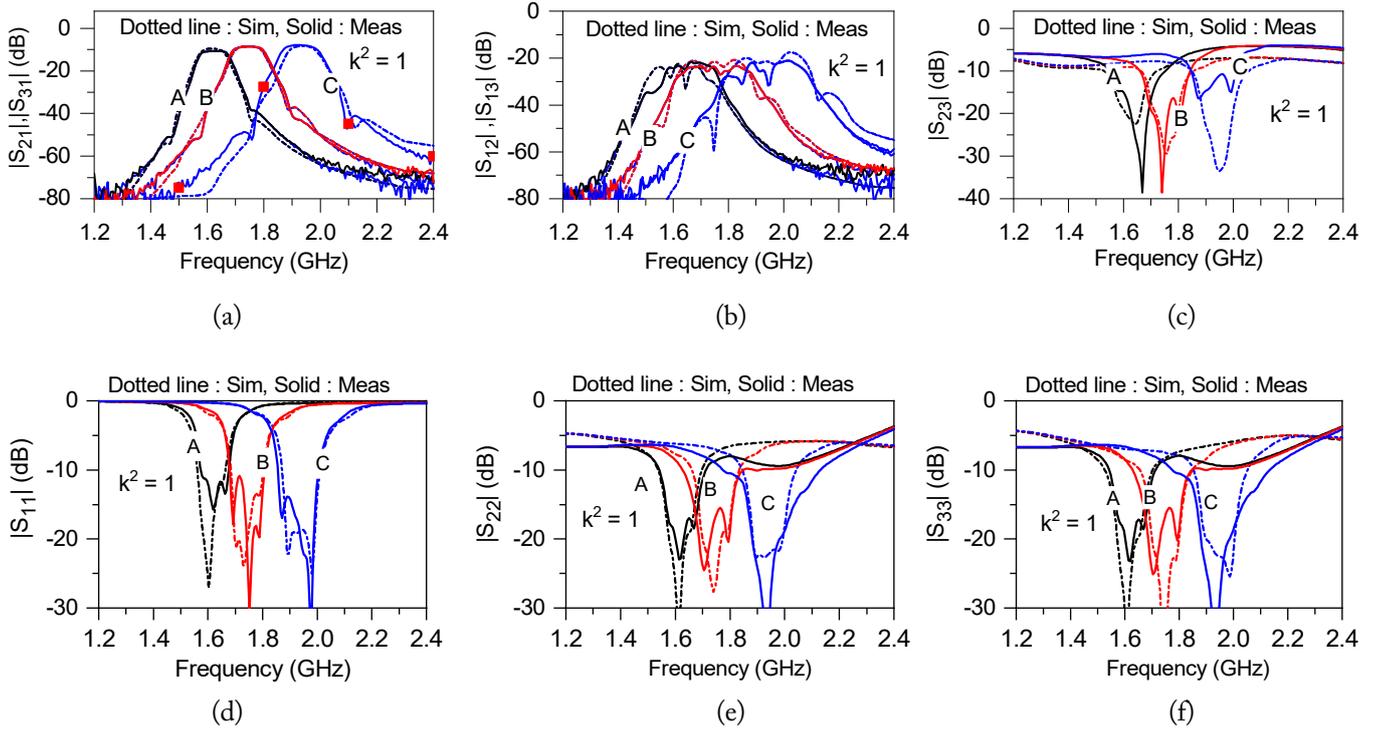


Fig. 9. Simulation and experimental S -parameters results for the fabricated NR-FPD with a tunable frequency: (a) $|S_{21}|$, $|S_{31}|$, (b) $|S_{12}|$, $|S_{13}|$, (c) $|S_{23}|$, (d) $|S_{11}|$, (e) $|S_{22}|$, and (f) $|S_{33}|$.

Table 3. Measured results for the NR-FPD with an equal power division ratio ($k^2 = 1$)

	Tunable frequency state		
	A	B	C
Modulation parameters			
f_m (MHz)	80	88	88
V_m (V)	2	2.70	3.20
$\Delta\varphi$ ($^\circ$)	35	36	37
Measured results			
V_{dc} (V)	0	2.40	6
f_0 (GHz)	1.62	1.75	1.95
$ S_{11} / S_{22} / S_{33} $ (dB)	>11.6 / 17.02 / 17.2	>10.90 / 15.5 / 15.45	>14.4 / 17.1 / 17.2
$ S_{21} / S_{31} @ f_0$ (dB)	8.71 / 8.73	8.10 / 8.11	7.56 / 7.58
$ S_{21} $ and $ S_{31} $ (dB)	>21.60	>23.40	>21.20
$ S_{32} @ f_0$ (dB)	18.2	22.20	12.1
Insertion loss (dB)	<5.70	<5.09	<4.55
ISO @ f_0 (dB)	22.89	24.24	22.90
ISO @ all frequency (dB)	>20.6	>20.40	>21.20
BW_{3dB} (MHz)	110	120	131
$BW_{20dB-ISO}$ (MHz)	All freq (∞)	All freq (∞)	All freq (∞)
Frequency tunability range	1.62–1.95 GHz (0.33 GHz): 18.48%		

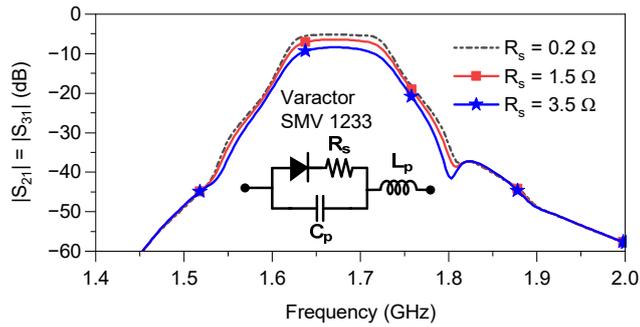


Fig. 10. Simulated results for the NR-FPD with different parasitic resistance (R_s) values of the varactor diode.

Table 4 compares the performance of the proposed NR-FPD with those described in previously published works [14–17]. Notably, these previously reported NR-FPDs [14–17] exhibited a high reverse ISO only at the center frequency and the 20-dB isolation bandwidth remained between 5 and 96 MHz. In contrast, this paper proposes an NR-FPD with frequency tunability and an ultrawide high reverse ISO bandwidth. The experimental results show that attenuation exceeded 20 dB in the reverse direction for all operating frequency ranges.

IV. CONCLUSION

This paper proposes a novel design of a multi-functional NR-FPD that combines the functions of a tunable bandpass filter, a power divider with an arbitrary PDR, and an isolator into one circuit. The achievement of an ultrawide high reverse isolation bandwidth was facilitated by properly selecting the modulation parameters of the time-modulated resonators. Moreover, the proposed NR-FPD features a low transmission IL in the forward direction and ultrawide high reverse isolation bandwidth in the backward direction, with tunable frequency functionalities. To validate the performance experimentally, a prototype of the NR-FPD was designed. The results show that the measured S -parameters had excellent agreement with the simulation.

Table 4. Performance comparison with previously published works

Study	FTR (GHz)	No. of TVR	IL (dB)	RL (dB)	ISO @ f_0 (dB)	BW _{3dB} (MHz)	BW _{20dB-ISO} (MHz)	Circuit size
Chaudhary et al. [14]	1.46	2	2.94	>15	28.77	130	50	$0.80\lambda_g \times 0.34\lambda_g$
Zhao et al. [15]	2.38–2.42 (1.66%)	5	4.8–5.9	>12	19.2–24	NA	5	$2.72\lambda_g \times 2.72\lambda_g$
Zang et al. [16]	2.45	6	8	>12	6.8–62.1	90	NA	NA
Chaudhary and Jeong [17]	1.66–1.98 (17.5%)	6	3.88–5.04	>11.44	20.2	100–112	70–96	$0.62\lambda_g \times 0.32\lambda_g$
This work	1.62–1.95 (18.48%)	4	4.55–5.70	>10.9	23.4–31.2	110–131	∞	$0.63\lambda_g \times 0.41\lambda_g$

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