ISSN 2287-4348

ISITC 2014

2014 International Symposium on Information Technology Convergence

KISM Fall Conference 2014

2014 Korean Institute of Smart Media Fall Conference

(Vol.3 No.2)

October 30-31, 2014 Chonbuk National University, Korea http://kism.or.kr/ISITC2014



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	Han Hai1, Moon Ho Lee1, Yongchae Jeong1, Yier Yan2, Liting Huang2 and Jae Seung Yang3 1Division of Electronics Engineering, Chonbuk National University, Korea 2School of Mechanical and Electrical Engineering, Guangzhou University, China 3Computer Engineering Daejin University, Korea	
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Block Circulant Toeplitz Jacket Matrix for Correlated MIMO Channel

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Abstract-In this paper, we analyze the capacity of multiple-input multiple-output (MIMO) corrlated channels in the presence of fading correlation at both the transmitter and the receiver, assuming that the channel is unknown at the transmitter and perfectly known at the receiver. We apply the block circulant Jakcet matrix to the covariance of the channel matrix, which improve the performance of the system.

Index Terms-MIMO, Jacket matrix, channel capacity, block circulant matrix.

I. INTRODUCTION

Multiple-input multiple-output (MIMO) communication systems using multiple transmit and receive antennas promise high spectral efficiency and link reliability for wireless communications [1]. Although the linear growth of capacity with the number of antennas indicates the potential of MIMO systems, the true benefits of the use of multiple antennas may be limited by spatial fading correlation due to closely-spaced antenna configurations and poor scattering environments in realistic wireless channels [4],[5]. Since the pioneering work of [1][3] in the area of multiple-antenna communications predicted remarkable spectral efficiency of MIMO wireless systems in independent and identically distributed (i.i.d.) Rayleigh fading, much subsequent work has concentrated on characterizing MIMO capacity under correlated fading [4][5]. However, the exact analytical results for the capacity such as ergodic (or mean) capacity, capacity variance, and outage capacity (i.e., capacity versus outage probability) have been known for only a few special cases, largely due to mathematical intractability (see, e.g., [3], [6] for i.i.d. flat Rayleigh fading and [2] for a one-sided correlated MIMO channel). For a more general case of correlated fading at both the transmitter and the receiver, which we will refer to as doubly correlated MIMO channels in the paper, some limited results are available: the capacity distribution for a small number of antennas are the numbers of transmit and receive antennas, respectively), upper and lower bounds on the ergodic capacity, capacity statistics for the case with a large number of antennas, and the asymptotic mean and variance of the capacity in the limit as the number of antennas tends to infinity. The temporal behavior of the capacity was analyzed in [4] in terms of level crossing rates and average fade durations.

The remainder of this paper is organized as follows. The next section states system model. Section III introduces block circulant matrices to the correlated MIMO channel, which can improve the performance of the system.

II. SYSTEM MODEL

For a MIMO system with N_T transmit and N_R receive antennas, as shown in Figure 1, a narrowband time-invariant wireless channel can be represented by $N_R \times N_T$ deterministic matrix $H \in \mathbb{C}^{N_R \times N_T}$.



Fig. 1. Architecture of the MIMO channel.

Consider a transmitted symbol vector $x \in \mathbb{C}^{N_T \times 1}$, which is composed of N_T independent input symbols $x_1, x_2, \cdots, x_{N_T}$. Then, the received signal $x \in \mathbb{C}^{N_R \times 1}$ can be rewritten in a matrix form as follows:

$$y = \sqrt{\frac{E_x}{N_T}} H x + z \tag{1}$$

where $z = (z_1, z_2, \cdots, z_{N_r})^T \in \mathbb{C}^{N_R \times 1}$ is a noise vector, which is assumed to be zero-mean circular symmetric complex Gaussian (ZMCSCG). E_x is the energy of the transmitted signals. Note that the noise vector z is referred to as circular symmetric when $e^{j\theta}z$ has the same distribution as z for any θ . The autocorrelation of transmitted signal vector is defined as

$$R_{xx} = Exx^{H}.$$
 (2)

Note that $Tr(R_{xx}) = N_T$ the transmission power for each transmit antenna is assumed to be 1.

In general, the MIMO channel gains are not independent and identically distributed (i.i.d.). The channel correlation is closely related to the capacity of the MIMO channel. In the sequel, we consider the capacity of the MIMO channel when the channel gains between transmit and received antennas are correlated. When the SNR is high, the deterministic channel capacity can be approximated as

$$C \approx \max_{Tr(R_{xx})=N} \log_2 \det(R_{xx}) + \log_2 \det(\frac{E_x}{N\mathbf{N}_0} \mathbf{H}_w \mathbf{H}_w^H)$$
(3)

From Equation (3), we can see that the second term is constant, while the first term involving $det(R_{xx})$ maximized when $R_{xx} = I_N$. Consider the following correlated channel model:

$$H = R_r^{1/2} H_w R_t^{1/2} (4)$$

where R_t is the correlation matrix, reflecting the correlations between the transmit antennas (i.e., the correlations between the column vectors of H), R_r is the correlation matrix reflecting the correlations between the receive antennas (i.e., the correlations between the row vectors of H), and H_w denotes the i.i.d. Rayleigh fading channel gain matrix. The diagonal entries of R_t and R_r are constrained to be a unity. Then, the MIMO channel is given as

$$C = \log_2 \det \left(I + \frac{E_x}{NN_0} R_r^{1/2} H_w R_t H_w^H R_r^{H/2} \right)$$
(5)

The narrorband MIMO radio channel $H \in \mathbb{C}^{M \times N}$ which describes the connection between the MS and the BS can be expressed as

$$R_T = \begin{pmatrix} \alpha_{11} & \alpha_{12} & \cdots & \alpha_{1N} \\ \alpha_{21} & \alpha_{22} & \cdots & \alpha_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ \alpha_{M1} & \alpha_{M2} & \cdots & \alpha_{MN} \cdots \end{pmatrix}.$$

where α_{mn} is the complex transmission coefficient from antenna n at the MS to antenna m at the BS. For simplicity, it is assumed that α_{mn} is complex Gaussian distributed with identical average power.

The spatial correlation matrix at the MS and the BS and is given by

$$R_{MIMO} = R_R \otimes R_T, \tag{6}$$

where \otimes represents the Kronecker product. This has also been confirmed in [7].

III. BLOCK CIRCULANT JACKET MATRIX FOR CORRELATED MIMO CHANNEL

The bivariate or two-dimensional Gaussian PDF. The mean m_x and the covariance matrix M for this case are

$$m_x = \begin{pmatrix} m_1 \\ m_2 \end{pmatrix}, M = \begin{pmatrix} \sigma_1^2 & \mu_{12} \\ \mu_{12} & \sigma_2^2 \end{pmatrix},$$

where the joint central moment μ_{12} is defined as

$$\mu_{12} = E[(X_1 - m_1)(X_2 - m_2)]. \tag{7}$$

It is convenient to define a normalized covariance

$$\rho_{ij} = \frac{\mu_{ij}}{\sigma_i \sigma_j}, i \neq j \tag{8}$$

where ρ_{ij} satisfies the condition $0 \le |\rho_{ij}| \le 1$. When dealing with the two-dimensional case, it is customary to drop the subscripts on μ_{12} and ρ_{12} . Hence the covariance matrix is expressed as

$$M = \begin{pmatrix} \sigma_1^2 & \rho \sigma_1 \sigma_2 \\ \rho \sigma_1 \sigma_2 & \sigma_2^2 \end{pmatrix}.$$

For example, in 2×2 correlated transmitter receiver setup, let $a = [w, x, y, z]^T$ be a vector of four complex zero-mean, unit variance independent random variables. Applying the Gaxpy algorithm

[6, p. 143], the lower-triangular matrix C, result of the Cholesky decomposition of Γ , is given by shown at the bottom of the page.

Defining $A = [\alpha_{11}, \alpha_{12}, \alpha_{21}, \alpha_{22}]^T$, the channel coefficients α_{ij} are generated as

$$A = Ca, \tag{9}$$

$$\begin{pmatrix} \alpha_{11} \\ \alpha_{12} \\ \alpha_{21} \\ \alpha_{22} \end{pmatrix} = C \begin{pmatrix} w \\ x \\ y \\ z \end{pmatrix}$$

Then we can have

$$\langle \alpha_{11}, \alpha_{11} \rangle = \frac{E[\alpha_{11}\alpha_{11}^*]}{\sigma_{\alpha_{11}}^2}$$
(10)

$$= \frac{E[\alpha_{11}w\alpha_{11}w]}{\sigma_{\alpha_{11}}^2}$$
(11)

$$= \frac{\sigma_{\alpha_{11}} E[ww]}{\sigma_{\alpha_{11}}^2}$$
(12)
= 1 (13)

since w has unit variance.

$$\langle \alpha_{11}, \alpha_{12} \rangle = \frac{E[\alpha_{11}\alpha_{12}^{*}]}{\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}}$$
(14)
$$= \frac{E[\sigma_{\alpha_{11}}w\left(\sigma_{\alpha_{12}}\rho^{*}w + \sigma_{\alpha_{12}}\sqrt{1-|\rho|^{2}}x\right)^{*}]}{\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}}$$
(15)
$$= \frac{\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}}{\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}}$$
(15)

$$= \frac{\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}\rho E[ww] + \sigma_{\alpha_{11}}\sigma_{\alpha_{12}}\sqrt{1 - |\rho|^2 E[wx]}}{\sigma_{\alpha_{11}}\sigma_{\alpha_{12}}}$$
(16)
$$= \rho$$
(17)

$$\langle \alpha_{11}, \alpha_{21} \rangle = \frac{E[\alpha_{11}\alpha_{21}^*]}{\sigma_{\alpha_{11}}\sigma_{\alpha_{21}}}$$
(18)
$$= \frac{E[\sigma_{\alpha_{11}}w \left(\sigma_{\alpha_{21}}\mu^*w + \sigma_{\alpha_{21}}\sqrt{1 - |\mu|^2}y\right)^*]}{\sigma_{\alpha_{11}}\sigma_{\alpha_{21}}}$$
(19)
$$= \frac{\sigma_{\alpha_{11}}\sigma_{\alpha_{21}}\mu E[ww^*] + \sigma_{\alpha_{11}}\sigma_{\alpha_{21}}\sqrt{1 - |\mu|^2}E[wy^*]}{\sigma_{\alpha_{11}}\sigma_{\alpha_{21}}}$$
(20)
$$= \mu$$
(21)

Therefore, we have

$$\rho_{ij} = \frac{\mu_{ij}}{\sigma_i \sigma_j}.$$
(22)

We will apply block circulant Jakcet matrix (BCJM) to improve time-invariant Gaussian MIMO channel capacity. Simulation computes the ergodic MIMO channel capacity when there exists a correlation between the transmit and receive antennas, with the following channel correlation matrices: $R_r = I_4$ and.

Case 1: Toeplitz channel matrix

$$R_T = \begin{pmatrix} \rho^0 & \rho^1 & \rho^2 & \rho^3 \\ \rho^3 & \rho^0 & \rho^1 & \rho^2 \\ \rho^2 & \rho^3 & \rho^0 & \rho^1 \\ \rho^1 & \rho^2 & \rho^3 & \rho^0 \end{pmatrix}.$$

 $R_r = I_4$ states that no correlation exists between the receive antennas. Figure has been generated by program , from which it



Fig. 2. Channel capacity versus SNR.



Fig. 3. Comparison of 4×4 MIMO and Block Diagonal 4×4 MIMO Symbol Error Rate.

can be shown that a capacity of 3.3 bps/Hz is lost due to the channel correlation when SNR is 18dB.

Case 2: Block circulant Jakcet matirx.

We have the R is a Block circulant matrix.

$$R = \left(\begin{array}{ccc} 1 & 1 & & \rho \left(\begin{array}{c} -1 & -1 \\ 1 & -1 & & \rho \end{array} \right) \\ \rho^* \left(\begin{array}{c} -1 & -1 \\ -1 & 1 \end{array} \right) & 1 & 1 \\ -1 & 1 \end{array} \right), |\rho| \le 1$$

From Fig. 2 and Fig. 3, we observe that the block circulant Kronecker channel capacity could improve than conventional MIMO as an efficient capacity achieving scheme at high signal-to-noise ratio regime. Fig. 3 shows the average BER performance versus input SNR for comparing the proposed transceiver scheme with the existing transceiver algorithms. It can be seen that smaller correlation coefficients lead to a better performance. It shows the ability of



Fig. 4. CDF of channel capacity.

the proposed algorithm to deal with the channel correlation. Figure 4 shows the CDFs of the correlated 2×2 and 4×4 MIMO channel capacities, it is clear from figure that the MIMO channel capacity improves with increasing the number of transmit and receive antennas.

The simulation shows the significance of proposed system.

IV. CONCLUSION

In this paper, we have applied the block circulant jacket matrices into correlated MIMO channel, since the transform is jacket matrices, the inverse transform is easily obtained by the reciprocal and transpose operations. Furthre, it has a fast efficient algorithm. On the other hand, since it is block circulant matrix, it can easily get the covariance of the correlated MIMO channel, which lead to a better performance.

ACKNOWLEDGMENT

This work was supported by the MEST 2012-002512 NRF and Brain Korea 21 Plus Project, NRF, Korea, and Natural Science Foundation of Guangdong Province (S2011040004068), China, and the scientific research foundation for returned overseas Chinese Scholars, State Education Ministry.

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