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## A DESIGN OF COMPACT WIDEBAND NEGATIVE GROUP DELAY NETWORK USING CROSS COUPLING

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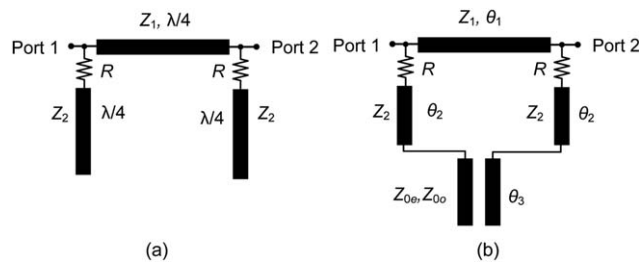
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**ABSTRACT:** This article presents a novel approach to the design of a compact wideband negative group delay (NGD) network using cross coupling between open stubs. The NGD time can be controlled by external series resistors, whereas the NGD bandwidth can be controlled by the coupling coefficient between open stubs. To verify the design concept, the NGD network operating at center frequency of 1.96 GHz was designed and fabricated. From the measurement results, a maximum achievable NGD time of  $-1.1 \pm 0.2$  ns was obtained over a 410 MHz BW with a maximum signal attenuation of 29.23 dB. © 2014 Wiley Periodicals, Inc. *Microwave Opt Technol Lett* 56:2495–2497, 2014; View this article online at [wileyonlinelibrary.com](http://wileyonlinelibrary.com). DOI 10.1002/mop.28627

**Key words:** cross coupling; negative group delay; wideband

### 1. INTRODUCTION

In recent years, there has been an increasing amount of research on negative group delay (NGD) networks due to their interesting characteristics of time advancement in wave propagations [1–7]. The NGD, being a counterintuitive phenomenon; can be observed in certain materials as well as artificial structures within limited frequency bands under a signal attenuation ( $S_{21}$ ) condition/negative refractive index [2], where it is equivalent to



**Figure 1** Structure of NGD networks: (a) conventional [6] and (b) proposed structure of wideband NGD network

an increasing phase with frequency. The NGD networks have been implemented in electronic circuitry and have been applied to various practical communication systems [3–7].

Recently, a new and interesting application of the NGD network for the realization of non-Foster reactive elements, such as a negative capacitance or inductor, has been reported in [8]. It has opened a door for new application fields of NGD networks, and can also be extended to electromagnetic (EM) applications such as increasing the bandwidth of artificial magnetic conductors by loading them with NGD networks as non-Foster elements. In RF and microwaves, the series and parallel resistor-inductor-capacitor (RLC) resonators are widely used to design active/passive NGD networks [3–7, 9]. To overcome the limited availability problem of lumped elements in RF and microwave, NGD networks using distributed elements have also been presented in literature [3, 7]. However, these conventional NGD networks suffer from a narrow NGD bandwidth. Recently, a passive NGD network with an enhanced bandwidth based on asymmetrical directional coupler has been reported [10]. However, this structure requires optimization methods to get the coupling coefficients of multisection directional couplers.

In this article, a novel method to design a distributed transmission line NGD networks with enhanced bandwidth is presented. The bandwidth of the proposed network can be controlled by a coupling coefficient between open stub resonators.

### 2. PROPOSED STRUCTURE OF TERMINATION NETWORKS

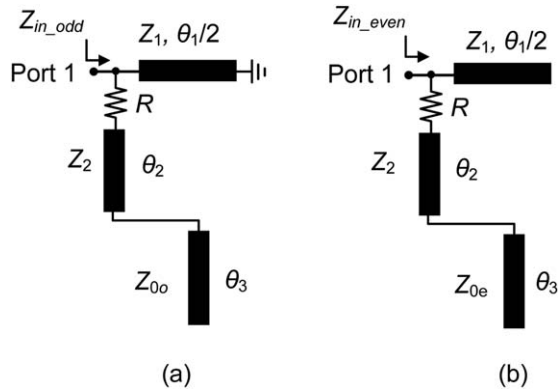
Figure 1(a) shows the conventional structure of NGD networks, which do not have coupling between two open stub resonators [6]. Figure 1(b) shows the proposed structure of NGD networks, which consists of resistor-connected stubs with a characteristic impedance  $Z_2$  and an electrical length  $\theta_2$ , a coupled line with characteristic impedances  $Z_{0e}$  and  $Z_{0o}$ , and electrical length  $\theta_3$ , and through line with a characteristic impedance  $Z_1$  and electrical length  $\theta_1$ . As the proposed NGD structure is symmetrical with respect to the center through line, odd- and even-mode analyses can be applied to find the performance of proposed circuit.

Under the odd-mode excitation, the proposed NGD structure can be represented as the equivalent half circuit shown in Figure 2(a). The odd-mode input impedance is given as shown in (1).

$$Z_{in\_odd} = \frac{Z_1 \tan(\theta_1/2)(A + jRB)}{RB + j(Z_1 B \tan(\theta_1/2) - A)} \quad (1)$$

where

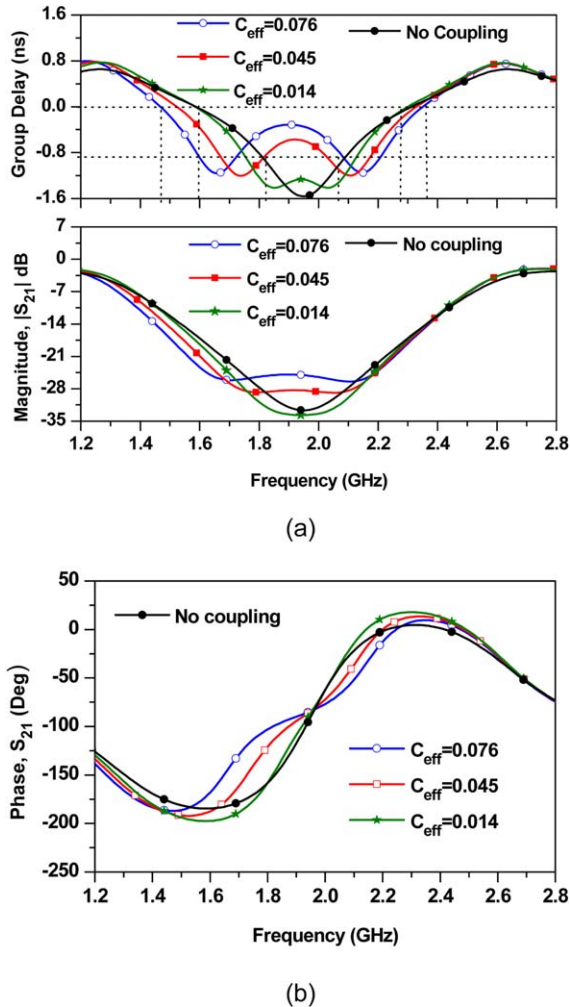
$$A = Z_2 Z_{0o} \cot \theta_3 - Z_2^2 \tan \theta_2 \quad (2a)$$



**Figure 2** The equivalent half circuits under odd- and even-mode excitations: (a) odd-mode excitation and (b) even-mode excitation

$$B = Z_2 + Z_{0o} \cot \theta_3 \tan \theta_2 \quad (2b)$$

Under the even-mode excitation, the proposed NGD network can be represented as the equivalent half circuit shown in Figure 2(b). The even-mode input impedance is given as shown in (3).



**Figure 3** Simulated results of proposed NGD network: (a) GD/magnitude characteristics and (b) phase characteristics of  $S_{21}$ . [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

$$Z_{in\_even} = \frac{Z_1 \cot(\theta_1/2)(C - jRD)}{RD - j(Z_1 D \cot(\theta_1/2) - C)} \quad (3)$$

where

$$C = Z_2^2 \tan \theta_2 - Z_2 Z_{0e} \cot \theta_3 \quad (4a)$$

$$D = Z_2 + Z_{0e} \cot \theta_3 \tan \theta_2 \quad (4b)$$

Using these odd- and even-mode impedances [11], the  $S$ -parameters of the proposed circuit are given as shown in (5).

$$S_{11} = S_{22} = \frac{Z_{in\_even} Z_{in\_odd} - Z_0^2}{(Z_{in\_even} + Z_0)(Z_{in\_odd} + Z_0)} \quad (5a)$$

$$S_{21} = S_{12} = \frac{(Z_{in\_even} - Z_{in\_odd})Z_0}{(Z_{in\_even} + Z_0)(Z_{in\_odd} + Z_0)} \quad (5b)$$

where  $Z_0$  is the port impedance. The group delay (GD) of the proposed circuit can be obtained using the following well-known relation.

$$\tau_g = -\frac{d\angle S_{21}}{d\omega} = -\frac{d}{d\omega} \left( \tan^{-1} \frac{\text{Im}(S_{21})}{\text{Re}(S_{21})} \right) \quad (5)$$

where  $\text{Im}(S_{21})$  and  $\text{Re}(S_{21})$  are the imaginary and real parts of the transmission coefficient ( $S_{21}$ ), respectively. The coupling coefficient of the coupled line in the proposed circuit is defined as shown in (7).

$$C_{\text{eff}} = \frac{Z_{0e} - Z_{0o}}{Z_{0e} + Z_{0o}} \quad (6)$$

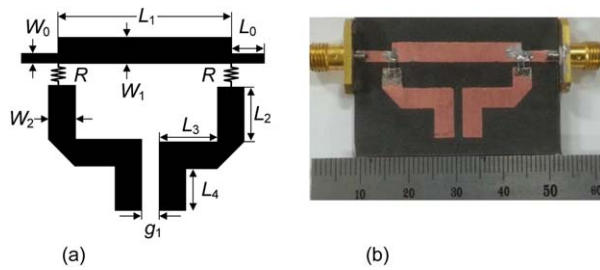
For the design graph, the GD, magnitude, and phase characteristics of the transmission coefficient ( $S_{21}$ ) are plotted in Figure 3 for different values of  $C_{\text{eff}}$ . For this purpose, the circuit elements of the proposed circuit are assumed to be  $Z_1 = Z_2 = 35 \Omega$ ,  $R = 3.5 \Omega$ ,  $\theta_1 = 90^\circ$ , and  $\theta_2 = \theta_3 = 45^\circ$  at the center frequency ( $f_0$ ) for simplicity. The different values of  $C_{\text{eff}}$  according to the combination of  $Z_{0e}$  and  $Z_{0o}$  are given in Table 1. As seen in Figure 3(a), the NGD bandwidth can be enhanced by increasing  $C_{\text{eff}}$  of the coupled lines. As compared to the NGD network without coupling, the proposed network has two poles in the NGD time, which helps to enhance the NGD bandwidth. However, the flatness of NGD is degraded. Therefore, there is a trade-off between the NGD magnitude flatness,  $S_{21}$  magnitude flatness, and the NGD bandwidth. Figure 3(b) shows the phase characteristics of the proposed wideband NGD network under the different values of  $C_{\text{eff}}$ . As seen from this figure, the slope of  $S_{21}$  is positive over a wide frequency range, which signifies the presence of NGD over a wide bandwidth.

### 3. EXPERIMENTAL VERIFICATION

To verify the design method of the proposed structure, the NGD network with a GD of  $-1.2$  ns operating at  $f_0 = 1.96$  GHz was

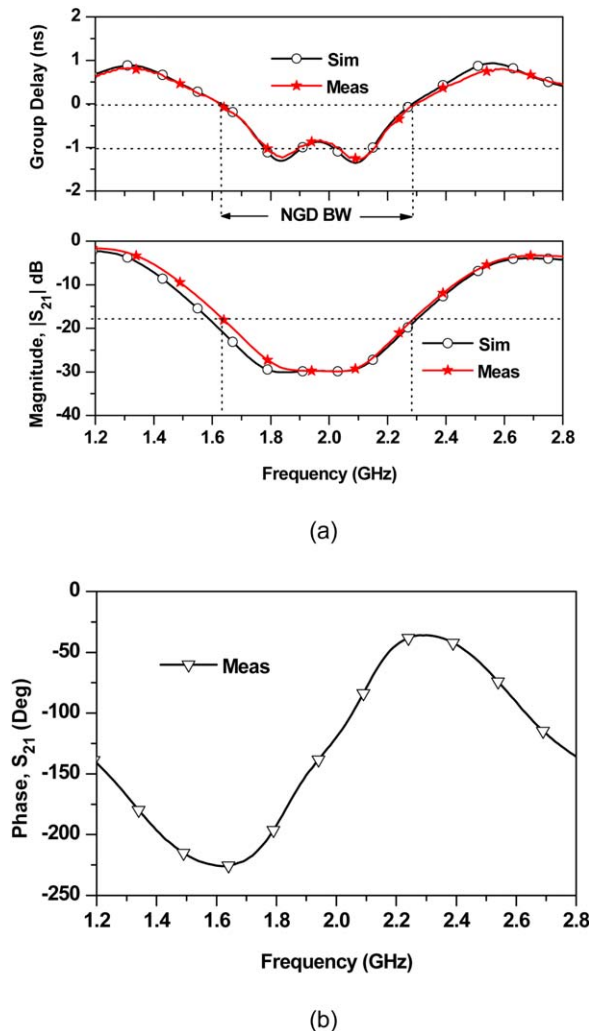
**TABLE 1** Odd- and Even-Mode Impedances of the Coupled Lines

$Z_{0e}$ ( $\Omega$ )	$Z_{0o}$ ( $\Omega$ )	$C_{\text{eff}}$
35	30	0.076
35	32	0.045
35	34	0.014
35	35	No coupling



**Figure 4** (a) EM simulation layout and (b) photograph of fabricated wideband NGD network. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

designed and fabricated. The EM simulation layout of the proposed network is shown in Figure 4(a). The circuit was fabricated on a Rogers RT/Duroid 5880 substrate with a dielectric constant ( $\epsilon_r$ ) of 2.2 and a thickness ( $h$ ) of 31 mils. The EM simulation was performed using HFSS v15. The parameters of the fabricated circuit after the EM simulation are given as:  $R = 3.5 \Omega$ ,  $W_0 = 2.4$ ,  $L_0 = 5$ ,  $W_1 = 4.20$ ,  $L_1 = 28$ ,  $W_2 = 4.2$ ,  $L_2 = 4.4$ ,  $L_3 = 11$ ,  $L_4 = 6.30$ , and



**Figure 5** Simulation and measurement results: (a) GD/magnitude characteristics and (b) phase characteristics of  $S_{21}$ . [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

$g_1 = 1.8$  (unit: millimeter). A photograph of the fabricated circuit is shown in Figure 4(b) and the overall circuit size is  $40 \times 35 \text{ mm}^2$ .

Figure 5(a) shows the simulation and measurement results of the proposed NGD network. As seen in these figures, the measurement results are in good agreement with the simulation results. From the measurements, a maximum achievable NGD value of  $-1.1 \pm 0.1 \text{ ns}$  over the frequency range of 1.76–2.75 GHz was obtained, which shows the widest bandwidth as compared to previous works [2, 6, 7]. Therefore, NGD-bandwidth product of the proposed circuit is given as 0.451. The maximum signal attenuation ( $S_{21}$ ) was found to be 29.30 dB at  $f_0 = 1.96 \text{ GHz}$ . Figure 5(b) shows the measured phase characteristics of  $S_{21}$ , where the phase slope is positive over a certain frequency range which can be used for the wideband phase compensation.

#### 4. CONCLUSION

In this article, the design of a compact wideband NGD network is presented. The NGD bandwidth can be controlled by the changing coupling coefficient between open stubs. For the experimental verification, the NGD network operating at a center frequency of 1.96 GHz was designed and fabricated. The measurement results were in good agreement with the simulations. The proposed network can provide a wideband NGD, is simple to design and is expected to be applicable for wideband communication systems.

#### ACKNOWLEDGMENT

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